Short note High-spin states in ¹⁶⁰Lu

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Abstract. High-spin states of ¹⁶⁰Lu have been studied through the ¹⁴⁴Sm(¹⁹F, 3n) reaction. The previously known $\pi h_{11/2} \otimes v i_{13/2}$ yrast band is extended from $I^{\pi} = 21^{-}$ to 25^{-} and a four quasiparticle band with configuration $\pi h_{11/2}[523]7/2^{-} \otimes v h_{9/2}[521]3/2^{-} \otimes (v i_{13/2})^2$ is reported.

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The systematic features of signature inversion of the $\pi h_{11/2} \otimes v i_{13/2}$ band in the deformed odd-odd nuclei around A = 160 have been studied extensively in recent years [1–8], and it has been established that, with increasing spin, the level staggering changes from inverted to normal signature dependence, and the spin, at inversion point, decreases with increasing neutron number Nin a chain of isotopes and increases with increasing proton number Z in a chain of isotones [2]. However, the existing data [9] shows that the variation pattern of the level staggering of the $\pi h_{11/2} \otimes v i_{13/2}$ band in ¹⁶⁰Lu is somewhat different from the general pattern described above. The inversion point has not been observed and the level staggering does not show the tendency towards the restoration of normal signature dependence at higher spins for the $\pi h_{11/2} \otimes vi_{13/2}$ band in ¹⁶⁰Lu. One of the motivations of the present study is to explore to what extent the variation behavior of the level staggering for the $\pi h_{11/2} \otimes v i_{13/2}$ band in $^{160}\mathrm{Lu}$ is different from the general pattern of the level staggering for the $\pi h_{11/2} \otimes v i_{13/2}$ bands in the other odd-odd nuclei around A = 160 mass region.

The high-spin states of ¹⁶⁰Lu were populated through the ¹⁴⁴Sm(¹⁹F, 3n)¹⁶⁰Lu fusion-evaporation reaction with 90 MeV ¹⁹F ions provided by the HI-13 tandem accelerator at CIAE in Beijing. The ¹⁴⁴Sm target is the same as the one used in the previous work on ¹⁶⁰Lu [9]. The γ - γ coincidence events were recorded with an array of eleven Compton-suppressed HpGe detectors. A total of ~ 80 × 10⁶ two-fold events were recorded for the off-line



Fig. 1. Level scheme of ¹⁶⁰Lu proposed in the present work.

analysis. The DCO γ - γ matrix were created sorting on one axis the detectors lying at $\theta_1 = 38^\circ$, 144° and on the other those at $\theta_2 = 90^\circ$ with respect to the beam direction. With setting gates on stretched quadrupole transitions, the theoretical DCO ratios $I_{\gamma \text{gate}} = \theta_2(\theta_1)/I_{\gamma \text{gate}} = \theta_1(\theta_2)$ are ≈ 1 for stretched quadrupole transitions and ≈ 0.5 for

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Table 1. The experimental data obtained from the present work. The γ -ray intensities were normalized to the 247.6 keV transition $(12^- \rightarrow 11^-)$, which is assumed to be 1000. In extracting the experimental B(M1)/B(E2) ratios, the mixing ratio δ is assumed to be zero.

Band number	E_{γ} (keV)	$(I^{\pi})_{\mathrm{i}} \rightarrow (I^{\pi})_{\mathrm{f}}$	I_{γ}	Branching ratio	DCO ratio	$\frac{B(M1)/B(E2)}{(\mu_N^2/e^2b^2)}$
A	252.5	$(11^{-}) \rightarrow (9^{-})$	975		0.96(7)	(* 2.1)
	325.9	$(12^{-}) \rightarrow (10^{-})$	82	0.08(1)	1.30(47)	2.10(0.25)
	247.6	$(12^{-}) \rightarrow (11^{-})$	1000	· · · ·	0.81(4)	· · · · ·
	407.6	$(13^{-}) \rightarrow (11^{-})$	500	0.91(9)	1.25(11)	2.12(0.17)
	159.6	$(13^{-}) \rightarrow (12^{-})$	547		0.65(5)	
	464.2	$(14^{-}) \rightarrow (12^{-})$	210	0.27(3)	0.94(36)	1.97(0.21)
	304.5	$(14^{-}) \rightarrow (13^{-})$	767		0.78(5)	
	537.5	$(15^{-}) \rightarrow (13^{-})$	639	1.2(2)	1.21(9)	2.05(0.28)
	232.7	$(15^{-}) \rightarrow (14^{-})$	528		0.55(4)	
	563.6	$(16^{-}) \rightarrow (14^{-})$	287	0.48(6)	1.36(19)	2.28(0.30)
	330.6	$(16^{-}) \rightarrow (15^{-})$	598	<i>.</i>	0.74(5)	<i>.</i>
	617.5	$(17^{-}) \rightarrow (15^{-})$	542	1.2(2)	1.06(9)	2.31 (0.31)
	286.5	$(17^{-}) \rightarrow (16^{-})$	473	(-)	0.54(5)	
	642.7	$(18) \rightarrow (16)$	371	1.1(1)	1.12(15)	1.58(0.19)
	356.0	$(18) \rightarrow (17)$ $(10^{-}) \rightarrow (17^{-})$	372	1 C (9)	0.71(6)	1.07(0.96)
	009.9 212 5	$(19) \rightarrow (17)$ $(10^{-}) \rightarrow (18^{-})$	370	1.0(2)	1.10(15)	1.97(0.26)
	515.5 600 7	$(19) \rightarrow (10)$ $(20^{-}) \rightarrow (18^{-})$	230	0.87(11)	0.01(0) 1.20(20)	9.25 (0.21)
	285.2	$(20^{-}) \rightarrow (10^{-})$	$240 \\ 275$	0.87 (11)	1.39(29) 0.58(7)	2.35(0.31)
	305.5 711.8	$(20) \rightarrow (19)$ $(21^{-}) \rightarrow (10^{-})$	275	15(9)	1.04(17)	2 30 (0 34)
	325.8	$(21) \rightarrow (19)$ $(21^{-}) \rightarrow (20^{-})$	$130 \\ 127$	1.0(2)	0.64(17)	2.55 (0.54)
	$\frac{525.8}{749.2}$	$(21) \rightarrow (20)$ $(22^{-}) \rightarrow (20^{-})$	106	0.83(12)	1.20(16)	2 60 (0 35)
	423.8	$(22^{-}) \rightarrow (21^{-})$	128	0.00 (12)	0.71(12)	2.00 (0.00)
	768.9	$(22^{-}) \rightarrow (21^{-})$	142	1.5(3)	1.20(16)	2.98(0.51)
	345.0	$(23^{-}) \rightarrow (22^{-})$	93	(0)	0.65(15))
	859.0	$(25^{-}) \rightarrow (23^{-})$	71		1.30(23)	
	<u> </u>	(20^+) (10^+)	280		0.63 (8)	
D	200.2	$(20^{+}) \rightarrow (19^{+})$ $(21^{+}) \rightarrow (10^{+})$	200	0.51(10)	1.36(20)	2.08 (0.60)
	202.2	$(21) \rightarrow (19)$ $(21^+) \rightarrow (20^+)$	216	0.01 (10)	1.30(23) 0.46(6)	2.38 (0.00)
	605.7	$(21^{+}) \rightarrow (20^{+})$	118	0.59(14)	1.26(27)	313(076)
	312.8	$(22^+) \rightarrow (21^+)$	200	0.00 (11)	0.47(26)	0.10 (0.10)
	633.9	$(23^+) \rightarrow (21^+)$	158	0.87(27)	1.35(31)	2.45(0.78)
	321.0	$(23^+) \rightarrow (22^+)$	182	0.01 (21)	0.55(10)	1 10 (0110)
	673.6	$(24^+) \rightarrow (22^+)$	149	0.69(21)	1.22(23)	3.19(0.96)
	352.6	$(24^+) \rightarrow (23^+)$	216	~ /	0.54(11)	
	703.4	$(25^+) \rightarrow (23^+)$	117	0.94(19)	1.33(32)	2.96(1.24)
	350.7	$(25^+) \rightarrow (24^+)$	125	. ,	0.67(28)	. ,
	733.2	$(26^+) \rightarrow (24^+)$	74	0.87(26)	1.21(45)	3.01 (0.90)
	383.4	$(26^+) \rightarrow (25^+)$	85		0.65(17)	× •
Linking	689.0	$(19^+) \rightarrow (18^-)$	173		0.64 (16)	
transitions	904.0	$(18^+) \rightarrow (17^-)$	171		0.55(12)	
		. / . /			× /	

pure dipole ones. The detectors were calibrated by using the ^{133}Ba and ^{152}Eu radioactive sources. The experimental results including transition energies, spin-parity assignments, γ -ray intensities, branching ratios, DCO ratios, and B(M1)/B(E2) ratios are listed in table 1, grouped in sequences for band A, B and linking transitions.

Figure 1 is the level scheme proposed in the present work and the sample coincidence spectra supporting the level scheme are shown in fig. 2. The $\pi h_{11/2} \otimes v i_{13/2}$ yrast band (band A) reported in [9] has been extended from $I^{\pi} = 21^{-}$ to 25^{-} and band B is a new band proposed in the present study. The spin and parity assignments of band A are adopted from [9]. Band B feeds band A via 689 and 905 keV transitions with DCO ratio of 0.64 and 0.55, respectively, indicating dipole character of both transitions. The competition of such energetic interband dipole transitions with the inband E2 and M1 transitions is indicative of E1 multipolarity of these interband transitions and thus the parity of band B is assumed to be positive. Band B decays through transitions 324, 602, 568, 517, 494, and 481 keV as shown in fig. 2(d). These lines could not be placed unambiguously into the level scheme.



Fig. 2. γ - γ coincidence spectra of band A (a, b) and band B (c, d).



Fig. 3. Plots of alignment versus frequency for the two rotational bands assigned to ¹⁶⁰Lu. J_0 (MeV⁻¹ \hbar^2) = 13.6 and J_1 (MeV⁻³ \hbar^4) = 154 for both band A and band B. The filled and open symbols refer to the even spin and odd spin, respectively.

The large alignment, as shown in fig. 3, and the highexcitation energy of band *B* suggest that band *B* is a four quasiparticle structure involving the coupling of the odd neutron and odd proton with a pair of aligned $i_{13/2}$ quasineutrons. Since the *BC* crossing occurs at $\hbar\omega \ge 0.35$ MeV in neighboring nuclei, the large alignment of band *B* is most likely contributed, in addition

to the alignments of odd neutron and odd proton, from the aligned $i_{13/2}$ quasineutron pair after AB crossing occurred in the unobserved initial part of band B. The AB crossing is not blocked and thus the odd neutron does not occupy the $i_{13/2}$ orbital in the four quasiparticle configuration of band B. $vi_{13/2}$ and $vh_{9/2}[521]3/2^{-1}$ are the orbitals which are close to the neutron Fermi surface in ¹⁶⁰Lu and bands built on these orbitals have been the only bands reported in 159 Yb [10] and 161 Yb [11]. It is reasonable to assume that the odd neutron in the configuration of band B occupies the $vh_{9/2}[521]3/2^-$ orbital. $\pi h_{11/2}[514]9/2^-, \pi h_{11/2}[523]7/2^-, \pi g_{7/2}[404]7/2^+,$ $\pi d_{3/2}[411]1/2^+$ and $\pi d_{5/2}[402]5/2^+$ are the orbitals close to the proton Fermi surface of ¹⁶⁰Lu. Due to the positiveparity assignment to band B and the neutron orbital assignment of $h_{9/2}[521]3/2^-$, only the orbitals with negative parity are the candidates of proton orbital in the configuration of band B. The experimental B(M1)/B(E2)values are compared with those calculated for different possible configurations of band B using the geometric model of Donäu and Frauendorf [12], as given in fig. 4. This comparison favors the configuration assignment $\pi h_{11/2}[523]7/2^- \otimes v h_{9/2}[521]3/2^- \otimes (v i_{13/2})^2$ to band B. The parameters used in the theoretical calculations are listed in table 2.

Figure 5 presents the level staggering for the $\pi h_{11/2} \otimes \upsilon i_{13/2}$ band in ¹⁶⁰Lu together with those of ¹⁶²⁻¹⁶⁸Lu and ¹⁵⁸⁻¹⁶⁴Tm. The common feature of the odd-odd isotopes of ¹⁶²⁻¹⁶⁸Lu and ¹⁶⁰⁻¹⁶⁴Tm is that the level staggering has



Fig. 4. Experimental B(M1)/B(E2) ratios as a function of spin for band B in 160 Lu. The solid curves correspond to calculations based on geometric model. $\pi h_{11/2}[514]9/2^{-1}$ \otimes $vh_{9/2}[521]3/2^{-1}$ \otimes $(vi_{13/2})^2;$ a) $vh_{9/2}[521]3/2^{-1}$ $(vi_{13/2})^2;$ $\pi h_{11/2}[523]7/2^{-1}$ \otimes b) \otimes c) $\pi g_{7/2}[404]7/2^+ \otimes vh_{9/2}[521]3/2^- \otimes (vi_{13/2})^2$

Table 2. Parameters used in the theoretical calculations of B(M1)/B(E2) ratios.

Bands	$i_{\rm n}(i_{\rm p})~(\hbar)$	$g_{ m n}(g_{ m p})$	$i_{ m nn}~(\hbar)$	Nuclei
$\pi h_{11/2}[514]9/2^{-1}$	2.2	1.32		¹⁶¹ Lu [13]
$\pi h_{11/2}[523]7/2^-$	3.2	1.41		¹⁵⁹ Lu [14]
$\pi g_{7/2}[404]7/2^+$	0.8	0.62		¹⁶¹ Lu [13]
$vh_{9/2}[521]3/2^-$	1.5	0.22	7.8	159 Er [15,16]
	$g_R = 0.44$	$Q_0 =$	4.37eb	

inverted signature dependence and the magnitude of level staggering increases with decreasing neutron number at lower spins. However, the variation pattern of the level staggering with the spin for ¹⁶⁰Lu is quite different from those of the other odd-odd isotopes. For $^{162\text{--}168}\mathrm{Lu}$ and $^{160\text{-}164}\mathrm{Tm},$ with increasing spin, the two signatures cross each other at an inversion point and the level staggering changes from inverted signature dependence to normal signature dependence, and the spin at inversion point increases with decreasing N. For ¹⁶⁰Lu, with increasing spin, the two signatures do not come to cross each other and, after passing through a minimum, the magnitude of the signature inverted level staggering increases and it shows no sign of the restoration of normal signature dependence at higher spins as observed in the other odd-odd isotopes. It is worthwhile to note that such a saddle-shape behavior in ¹⁶⁰Lu is not consistent with the understanding that the dominance of Coriolis effect and thus the normal signature dependence should be restored at higher spins. Similar phenomenon can also be seen in the Thulium chain of isotopes, as shown in fig. 5, but the saddle-shape behavior in 158 Tm is less pronounced comparing to that of 160 Lu.



Fig. 5. Level staggering for the $\pi h_{11/2} \otimes v i_{13/2}$ band in ¹⁶⁰Lu (present work) compared to those in the ¹⁶²⁻¹⁶⁸Lu and ¹⁵⁸⁻¹⁶⁴Tm isotopes, S(I) = E(I) - E(I-1) - [E(I+1) - E(I) + E(I-1) - E(I-2)]/2. The filled symbols refer to the even spins ($\alpha = 0$) and the open symbols to odd spins ($\alpha = 1$). The even spins are expected to be favored. Data sources: ¹⁶²Lu [5,17, 18], ¹⁶⁴Lu [5,19–21], ¹⁶⁶Lu [22–24], ¹⁶⁸Lu [25,26], ¹⁵⁸Tm [27, 28], ¹⁶⁰Tm [29], ¹⁶²Tm [30], ¹⁶⁴Tm [31].

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